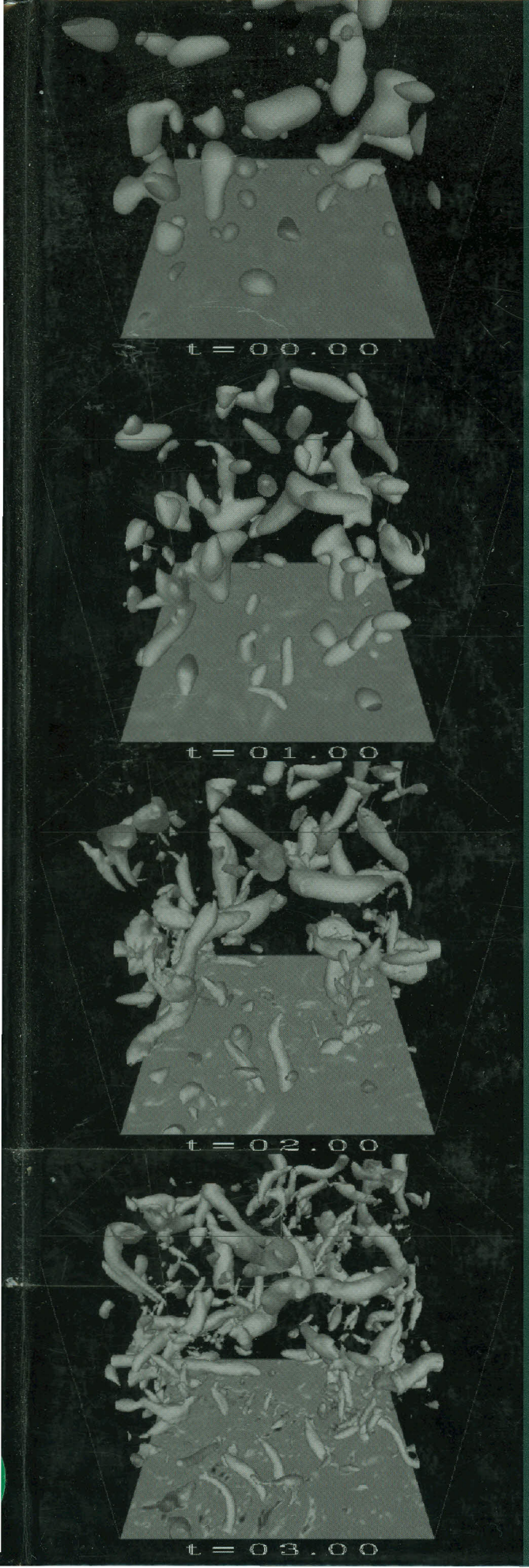
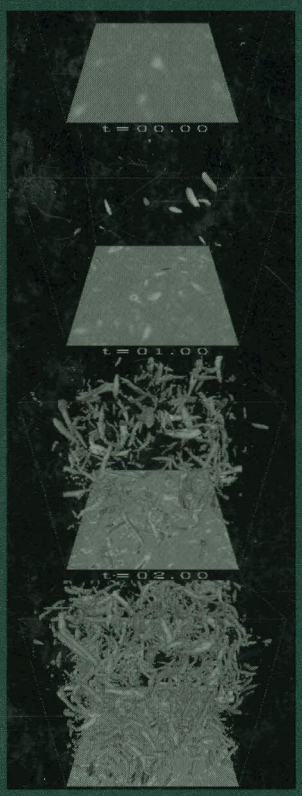


Large-Eddy Simulations of Turbulence



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Large-Eddy Simulations of Turbulence

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